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Effects of Chemical Short-Range Order and Temperature on Basic Structure Parameters and Stacking Fault Energies in Multi-Principal Element Alloys

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Abstract: In the realm of advanced material science, multi-principal element alloys (MPEAs) have emerged as a focal point due to their exceptional mechanical properties and adaptability for highperformance applications. This study embarks on an extensive investigation of four MPEAs-CoCrNi, MoNbTa, HfNbTaTiZr, and HfMoNbTaTi—alongside key pure metals (Mo, Nb, Ta, Ni) to unveil their structural and mechanical characteristics. Utilizing a blend of molecular statics and hybrid molecular dynamics/Monte Carlo simulations, the research delves into the impact of chemical short-range order (CSRO) and thermal effects on the fundamental structural parameters and stacking fault energies in these alloys. The study systematically analyzes quantities such as lattice parameters, elastic constants (C11, C12, and C44), and generalized stacking fault energies (GSFEs) across two distinct structures: random and CSRO. These properties are then evaluated at diverse temperatures (0, 300, 600, 900, 1200 K), offering a comprehensive understanding of temperature's influence on material behavior. For CSRO, CoCrNi was annealed at 350 K and MoNbTa at 300 K, while both HfMoNbTaTi and HfNbTaTiZr were annealed at 300 K, 600 K, and 900 K, respectively. The results indicate that the lattice parameter increases with temperature, reflecting typical thermal expansion behavior. In contrast, both elastic constants and GSFE decrease with rising temperature, suggesting a reduction in resistance to stability and dislocation motion as thermal agitation intensifies. Notably, MPEAs with CSRO structures exhibit higher stiffness and GSFEs compared to their randomly structured counterparts, demonstrating the significant role of atomic ordering in enhancing material strength.

Keywords: chemical short-range order; basic structural parameters; stacking fault energy; multi-principal element alloy

1. Introduction

Multi-principal element alloys (MPEAs) are an advanced class of metallic materials that have gained significant attention in materials science and engineering. The quest for materials that can withstand harsh environments, such as extreme heat, has led to the innovation of MPEAs, which differ from traditional alloys by using a balanced mix of multiple elements in equiatomic or near-equiatomic proportions at crystalline lattice sites, typically with either a face-centered cubic (FCC) or body-centered cubic (BCC) arrangement. The concept of equiatomic alloys forming stable solid solutions with high configurational entropies, resulting in the absence of complex phases and microstructures, was first introduced by Cantor et al. [1] and Yeh et al. [2], spurring further advancements in MPEAs. MPEAs have gained popularity owing to their fundamental properties, such as their high entropy effect, sluggish diffusion, cocktail effect, and lattice-distortion effect. The high configurational entropy notably decreases the Gibbs free energy within the system, enabling these alloys to avert the creation of brittle phases. This process, in turn, promotes the development of single-phase solid solutions, including FCC, BCC, and



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Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). hexagonal-close-packed (HCP) structures, within MPEAs [3]. Some MPEAs demonstrate substantially enhanced characteristics compared to conventional alloys. These mechanical characteristics are believed to be a direct result of the unique lattice structures and atomic interactions inherent in MPEAs, resulting in a rich tapestry of deformation mechanisms, including, but not limited to, intricate dislocation activities, stacking fault generation, and the formation of nanotwinning networks [4–6].

CoCrNi stands out as a key example of the diverse and enhanced structural properties that MPEAs can provide. MPEAs with an FCC structure, such as CoCrNi, demonstrate remarkable mechanical characteristics including high fracture toughness, work hardening, and resistance to shear-band formation [7]. As a subset of the Cantor alloy [1], CoCrNi is characterized by twinning-dominated deformation and exhibits superior mechanical properties, including an increased tensile strength of 1.3 GPa and a failure strain of 90% [8] at 77 K, thus outperforming the Cantor alloy in these respects which has a 1 GPa tensile strength and a 60% failure strain [9] at the same temperature.

In the meantime, a significant limitation of refractory metallic alloys lies in their weak resistance to oxidation at high temperatures. MPEAs offer a solution by incorporating high levels of elements that enhance oxidation resistance. Much of the research in this area focuses on merging elements with high melting points, which are known for their strength and thermal stability at elevated temperatures (such as Hf, Mo, Nb, Ta, W, and Zr), with elements that improve oxidation resistance, including Al, Cr, Ti, and Si [10]. Senkov et al. [11] successfully created two single-phase MPEAs, MoNbTaW and MoNbTaVW, with near-atomic compositions and a BCC structure. The exceptional strength, durability, and distinctive microstructural features of these alloys indicate their suitability for use in sectors such as aerospace, automotive, and defense, where materials must withstand extreme stress and temperatures. Wadsworth et al. [12] highlight that refractory alloys, including Mo, Nb, Ta, and W, offer extended creep resistance, oxidation tolerance, and improved welding methods, addressing brittleness and oxidation challenges, thus proving valuable for aerospace uses. The two equimolar refractory MPEAs, HfMoNbTaTi and HfNbTaTiZr, demonstrate substantial compressive yield strengths at room temperature, with HfMoNbTaTi exhibiting strengths between 1369–1713 MPa [13,14] and HfNbTaTiZr showing strengths in the range of 900–1073 MPa [15–19]. HfMoNbTaTi shows an impressive strength at high temperatures, reaching 699 MPa at 1473 K [13], while HfNbTaTiZr maintains a considerable ductility at room temperature, ranging from 11% to 25% [19–22].

Results emerging from these investigations underscore the considerable potential of these alloys, warranting increased exploration and focus. However, the processing and fabrication of these alloys present challenges, being both resource-intensive and costly. Nonetheless, atomistic calculations yield promising perspectives on the mechanical characteristics of various alloys, facilitating the prediction of plastic deformation behaviors that are congruent with experimental results [23–25]. An in-depth understanding of dislocation dynamics within metals is essential for a comprehensive grasp of plastic deformation phenomena. In metals, dislocation glide necessitates the disruption and reformation of bonds across crystalline glide planes, analogous to the shearing of a crystal along a plane [26]. The energy required for this shearing is encapsulated in the concept of generalized stacking fault energy (GSFE) [27,28]. GSFE has emerged as a pivotal parameter in the design and development of MPEAs with varied chemical compositions, proving to be invaluable for investigating the effects of different elemental concentrations and compositions on the behavior of plastic deformation [29]. Mayahi et al. [30] show that increasing the Co content in $AlCo_xCrFeNi$ enhances dislocation-mediated slip and martensitic transformation, influencing plastic deformation. Based on the evaluation of the GSFE curve, this research provides key insights for designing these alloys with an optimal balance of strength and ductility, notably in the AlCo₂CrFeNi alloy which exhibits superior properties. In CoCrFeNi, an increase in Cr and Fe reduces the GSFE while higher Co and Ni raise it, which impacts the vield stress [31].

MPEAs are characterized by the absence of chemical long-range ordering and often exhibit chemical short-range ordering (CSRO), a characteristic that has been experimentally validated [32,33]. CSRO in MPEAs significantly impacts their dislocation dynamics [34–36]. In MoNbTaW, CSRO significantly impacts the mobility of edge and screw dislocations, enhancing the mobility of edge dislocations while reducing the rate of double-kink nucleation in screw dislocations, an effect that diminishes at higher temperatures [36]. In HfNbTaZr, Chen et al. [22] investigated how annealing affects its nanostructure and mechanical properties, such as yield strength and ductility. They found that chemical short-range clustering (SRC) developed during annealing which significantly enhanced the alloy's strength. These SRCs impact the critically resolved shear stress, influencing the transition from ductile to brittle behavior. Zheng et al. [37] worked on TaNbTi and MoNbTi RMPEAs, and it was found that CSRO greatly impacts dislocation glide, with higher CSRO in MoNbTi leading to increased unstable stacking fault energies (USFE). This elevation in USFE necessitates greater stress for dislocation movement and results in hardening due to the compositional fluctuation.

In our work, we focus on four specific equi-molar, single-phase, single-crystalline MPEAs: CoCrNi, MoNbTa, HfMoNbTaTi, and HfNbTaTiZr. We aim to calculate their lattice parameters, elastic constants C₁₁, C₁₂, and C₄₄, and GSFE. These calculations directly correlate with key mechanical properties, including strength, ductility, and hardness. In particular, calculations of GSFE are crucial for improving the performance of materials, as they help identify deformation mechanisms like slip and twinning [38]. In this research, we analyzed specific parameters for two distinct structures: random and CSRO. Examining the properties of the CSRO structures offers valuable insights into the deformation mechanisms and behavior of materials [39–41]. To explore MPEAs exhibiting varying degrees of CSRO, we employed hybrid molecular dynamics (MD) and Monte Carlo (MC) simulations at different annealing temperatures. CoCrNi was annealed at 350 K and MoNbTa at 300 K, whereas both HfMoNbTaTi and HfNbTaTiZr were annealed at three different temperatures: 300 K, 600 K, and 900 K, respectively. Our focus was on deciphering the mechanical properties of these MPEAs under diverse temperature conditions. For some alloys, we gradually increased the environmental temperature from 300 K to 1200 K to assess the properties. Additionally, to contrast the behavior of MPEAs with that of pure metals, we also studied Mo, Nb, Ta, and Ni under the same escalating temperature range.

2. Materials and Methods

In this investigation, molecular statics simulations were conducted using LAMMPS [42]. The embedded-atom method (EAM) potentials are used to describe the interatomic potential. The atomic interactions within the CoCrNi system are represented by the EAM interatomic potential developed by Li et al. [43], which has been used in recent MD studies involving dislocation nucleation and motion [43,44]. The atomic interactions within HfNbTaTiZr and HfMoNbTaTi are represented by the EAM potential developed by Xu et al. [45]. In this study, the atomic interactions employed within MoNbTa were also developed by Xu et al. [46].

The EAM formulation that defines potential energy is given by [47]:

$$E = \frac{1}{2} \sum_{i}^{N} \sum_{\substack{j=1\\ j \neq i}}^{N_{\text{nei}}} V(R^{ij}) + \sum_{i} F(\bar{\rho}^{i})$$
(1)

where *N* represents the number of atoms, N_{nei} signifies the number of neighboring atoms of atom *i*, *V* refers to the pair potential, *F* is the embedding potential, $\bar{\rho}^i$ denotes the host electron density at atom *i*. Additionally, R^{ij} is the magnitude of vector \mathbf{R}^{ij} which points from atom *i* to atom *j*, i.e.,

$$\mathbf{R}^{ij} = \mathbf{R}^j - \mathbf{R}^i \tag{2}$$

$$\bar{\rho}^{i} = \sum_{\substack{j \\ j \neq i}}^{N_{\text{nei}}} \rho^{ij}(R^{ij}) \tag{3}$$

where ρ^{ij} is defined as the local electron density contributed by atom *j* to atom *i*. Here, formulations of *V* and ρ^{ij} only involve the *i* type of atom and the distance between atom *i* and its neighboring atom *j*, R^{ij} , regardless of the type of atom *j* is. For example, let atom *i* be Mo, then *V* and ρ^{ij} depend only on R^{ij} for any atom *j* which may be Nb or Ta. Thus, by using the EAM potentials for pure metals like Mo, Nb, or Ta, a unique "alloy potential" may be developed for every MPEA. For the four MPEAs considered here, this kind of potential will be utilized, as it has been to calculate GSFE in MoNbTi and NbTiZr [48], lattice distortion and chemical disorder in NbTiZr [49] and NbTaV [50,51], lattice parameters and stacking fault in Ti-Al-Nb systems [52], and high-temperature fatigue resistance of the polysynthetic twinned-TiAl single crystal [53].

To check the accuracy of the potential, density functional theory (DFT) simulations were conducted for lattice parameter and elastic constants C_{11} , C_{12} , and C_{44} with random structures to compare the results with atomistic calculations. Details can be found in Appendix A. Table 1 presents the results of atomistic calculations for the MPEAs with random structures at 0 K, which are in good agreement with those obtained from DFT calculations, with the exception of C_{44} , where a discrepancy is observed. Such discrepancies are known in many metals [54].

For this study, we utilized previously established CSRO structures for CrCoNi [55], as well as the quinary alloys HfMoNbTaTi and HfNbTaTiZr [45]. For this study, we constructed the CSRO structures for MoNbTa. Pure Mo samples were used to create MoNbTa MPEAs with completely random atomic distributions using Atomsk [56]. The Mo atoms were randomly substituted by Nb or Ta atoms until the desired equi-molar composition (Mo:Nb:Ta = 1:1:1) was reached. For the CSRO structures, first, using the hybrid MD/MC technique under the semi-grand-canonical ensemble at 1500 K, the chemical potential differences between Mo and Nb or Ta were determined to be $\Delta \mu_{\text{Nb-Mo}} = -0.8056 \text{ eV}$, $\Delta \mu_{\text{Ta-Mo}} = -1.26 \text{ eV}$, respectively. Next, we employed the hybrid MD/MC method under the variance-constrained semi-grand-canonical ensemble for annealing temperatures of 300 K for MoNbTa MPEA. For both random and CSRO structures, the Warren–Cowley (WC) parameters were calculated via

$$\alpha_{ij}^n = \frac{p_{ij}^n - c_j}{\delta_{ij} - c_j} \tag{4}$$

where *n* means the *n*th-nearest-neighbor shell of the central *i*-type atom, p_{ij}^n denotes the probability of a *j*-type atom being around an atom of type *i* within the *n*th shell, c_j is the concentration of *j*-type atom, and δ_{ij} is the Kronecker delta function [57,58].

In a completely random structure, the value of α_{ij}^n will be close to zero, whereas a higher magnitude value of α_{ij}^n would suggest a higher degree of CSRO. The positive value of α_{ij}^n indicates the segregation of the same species (i = j) whereas the negative value of α_{ij}^n corresponds to the local ordering of the different species ($i \neq j$).

In all alloys, we use "number+K+MDMC" to denote a structure obtained by hybrid MD/MC at a specific annealing temperature. For CoCrNi, one CSRO structure, annealed at 350 K [55], was considered. For this ternary, $\Delta \mu_{\text{Co-Ni}} = -0.021 \text{ eV}$, $\Delta \mu_{\text{Cr-Ni}} = 0.32 \text{ eV}$. Figure 1 shows the average α_{ij}^1 , for the 1st nearest neighbor, for the random and CSRO structure of MoNbTa generated at an annealing temperature of 300 K. The value for the random structure is close to zero, and the CSRO structure has a comparatively higher value, as expected. The positive value of α_{TaTa}^1 and the high negative values of α_{MoTa}^1 and α_{NbTa}^1 indicate that these pairs tend to segregate or form local ordering in the structure. In Figure 2, the atomistic structures of random and CSRO annealed at 300 K are presented.

For HfNbTaTiZr and HfMoNbTaTi, three different CSRO structures were used, which were annealed at temperatures of 300, 600, and 900 K respectively [45].



Figure 1. Pairwise chemical WC parameters α_{ij}^1 in MoNbTa.



Figure 2. Atomistic structures of MoNbTa with random and CSRO structure. Visualization is carried out in OVITO [59].

Table 1. Lattice parameters a_0 (in Å) and effective elastic constants C_{11} , C_{12} , and C_{44} (in GPa) of random structures for four MPEAs using three different methods: experiment (Exp), DFT, and EAM.

MPEA	Methods	<i>a</i> ₀	<i>C</i> ₁₁	<i>C</i> ₁₂	C ₄₄
	Exp	3.565 [60]			
CoCrNi	DFT	3.305 [61]	278.8 [62]	188.8 [62]	183.0 [<mark>62</mark>]
	EAM	3.55644	$\begin{array}{c} C_{11} \\ 278.8 [62] \\ 251.644 \\ 261.51 \\ 307.17 \\ \\ 209.95 \\ 201.42 \\ 172 [63] \\ 160.2 \\ 149.63 \end{array}$	178.246	95.134
	DFT	3.26	261.51	181.48	61.72
MoNbla	EAM	3.243	307.17	159.46	77.51
	Exp	3.305 [13,14]			
HfMoNbTaTi	DFT [45]	3.305	209.95	133.92	39.68
	EAM [45]	3.31	278.8 [62] 251.644 261.51 307.17 209.95 201.42 172 [63] 160.2 149.63	146.64	82
	Exp	3.304 [15]	172 [63]	116 [63]	28 [63]
HfNbTaTiZr	DFT [64]	3.457	160.2	124.4	62.4
	EAM [45]	3.405	149.63	111.83	64.67

The bulk energy for every cell size is calculated to obtain the lattice parameter a_0 of each atomic structure using a sequence of periodic simulated cells of different sizes. In the end, the cohesive energy, E_{coh} is obtained by dividing the total number of atoms in the cell by the least bulk energy among these cells. It has been shown that this strategy, known as the "energy-volume method" yields results that are almost the same as those obtained

using the "relaxation method" [65]. On the other hand, the stress–strain approach is used to determine the stiffness tensor C [66]. The effective elastic constants, C_{11} , C_{12} , and C_{44} , at finite temperatures were determined using the Born-matrix method [67]. GSFEs were obtained following our previous work [48].

3. Results and Discussions

3.1. Lattice Parameters

As previously mentioned, we determined the lattice parameter, a_0 , for both the random and CSRO structures in four MPEAs, CoCrNi, MoNbTa, HfNbTaTiZr, and HfMoNbTaTi, across a temperature range of 300 to 1200 K. Figure 3a illustrates the correlation between a_0 and temperature for CoCrNi with random and CSRO structures and Figure 3b displays MoNbTa in its random and CSRO states and the simple rules of mixtures (SROM) of MoNbTa. It was observed that a_0 exhibits an increase with the temperature rise. The expansion of a_0 in MPEAs with rising temperature is accentuated by the pronounced lattice distortions caused by the varying atomic sizes and potentials of their constituent elements [68]. The a_0 of the random and CSRO structures in CoCrNi and MoNbTa exhibit minimal differences in *a*₀ compared to their random counterparts, suggesting that chemical order may have a negligible effect on thermal expansion in these specific alloys. Mayahi [30] notes that the GSFE can be influenced by alloy composition and ordering, but does not significantly affect a_0 . Furthermore, by averaging the a_0 values of Mo, Nb, and Ta at each temperature, the lattice parameters a_0 for a random MoNbTa with SROM were determined. The graph unequivocally demonstrates that a random MoNbTa with SROM closely resembles the observed values and temperature patterns in the ternary MoNbTa's random and CSRO structures. The lattice parameter for the random MoNbTa with SROM exhibits smaller values compared to the random MoNbTa structure.

As displayed in Figure 3c, the progression of a_0 for HfMoNbTaTi MPEA at various temperatures reflects a similar increasing pattern to that seen in the previous two MPEAs. For HfMoNbTaTi, the random structure demonstrates a larger a_0 compared to the three CSRO structures—300KMDMC, 600KMDMC, and 900KMDMC—which show lower values. As the temperature climbs, these CSRO structures exhibit a consistent and collective increase in a_0 . In Figure 3d, the lattice parameters of HfNbTaTiZr in a random structure configuration are presented, demonstrating a consistent increase as the temperature rises.

For pure metals, as observed in Figure 3e, Mo, Ta, Ni, and Nb all show an increase in a_0 with temperature, with Mo showing the least change. This behavior reflects the inherent material properties of pure metals, where the atomic bonding and size dictate their thermal expansion characteristics [69]. The lesser change in Mo's a_0 could be due to its higher melting point and stronger bonds, which make it more resistant to thermal expansion. Using our interatomic potential, at 1200 K, Nb exhibited an unstable structure; thus, we did not calculate any properties for Nb at this high temperature.





(a) CoCrNi (Random and CSRO)

(b) MoNbTa (Random, CSRO, SROM)

Figure 3. Cont.



HfNbTaTiZr

300

600

Temperature (K)

900

1200



(e) Pure Metals

Figure 3. Relationship between lattice parameter and temperature of MPEAs and pure metals. Data for Mo, Nb, Ta, HfMoNbTaTi, and HfNbTaTiZr at 0 K are taken from previous work.

3.2. Elastic Constants

The elastic constant behavior with varying temperature has been exhibited in Figures 4-6. Three elastic constants (C_{11} , C_{12} , and C_{44}) have been explored in this study. Figures 4a–c illustrate all the elastic behavior trends for CoCrNi (random and CSRO), MoNbTa (random and CSRO), and random MoNbTa based on the simple rule of mixtures (SROM), Figure 5 illustrates all the elastic behavior trends for four structures of HfMoNbTaTi and HfNbTa-TiZr; Figure 6 illustrates all the elastic behavior trends for four pure metals (Mo, Nb, Ni, and Ta). In all figures, it is evident that, with temperature, the elastic constants tend to decrease. This behavior is consistent with the fundamental understanding of the fact that, as temperature increases, the atomic vibrations become more pronounced, leading to a reduction in the material's resistance to deformation, which is reflected in the decrease in elastic constants [37,70]. The elastic constants of the CSRO variants of CoCrNi and MoNbTa showed higher elastic constants than their random counterparts [71]. In the case of the elastic constant C₄₄, the CSRO and random structures of both MoNbTa and CoCrNi display a similar trend, but both structures of CoCrNi display a pronounced decrease compared to the MoNbTa structures. A comparative study of SROM behavior in MoNbTa with random and CSRO structures is shown in Figure 4. The MoNbTa SROM values are similar to the ternary MoNbTa structures in both the random and CSRO variations. Nevertheless, we are unable to draw firm conclusions from this comparison because these SROM values do not closely match any particular MoNbTa MPEA structure. As a result, it would appear that SROM inadequately represents all of the ternary configurations of MoNbTa. The C_{11} and C44 for MoNbTa SROM display higher values than random MoNbTa structure, whereas the C_{12} for MoNbTa SROM shows a lower value.

Similarly, the four configurations of HfMoNbTaTi and HfNbTaTiZr demonstrate a consistent downward trend in elastic constants as temperature increases. The elastic behavior across the four distinct atomic arrangements reveals a negligible variation. This uniformity in the reduction of elastic constants with temperature, observed in both random



and CSRO structures, implies that the alloy's inherent thermal response predominates over the influence of particular atomic configurations [72].

Figure 4. Relationship between elastic constants and temperature in CoCrNi and MoNbTa.



Figure 5. Relationship between elastic constants and temperature in HfMoNbTaTi and HfNbTaTiZr. Data at 0 K are taken from previous work [45].

Figure 6 indicates that the behavior of elastic constants in pure metals, specifically Mo, Nb, Ta, and Ni, parallels the patterns observed in MPEAs. Notably, the shear-related elastic constants, C_{12} and C_{44} , demonstrate minor variations across these metals when contrasted with the longitudinal elasticity constant, C_{11} . The graphs further reveal that Mo exhibits superior stiffness, which can be attributed to its robust atomic bonding and elevated melting temperature.



(c) C₄₄

Figure 6. Relationship between elastic constants and temperature in four pure metals. Data for Mo [48], Nb [48], and Ta [46] at 0 K are taken from previous work.

3.3. Generalized Stacking Fault Energy (GSFE)

GSFE provides an energy map which is critical for understanding the mechanical stability and slip behavior of MPEAs, influenced by their complex elemental interplay. In this study, GSFE curves were generated by shifting the top half of the samples along the *z*-axis within the {111} or {110} plane. For robust statistical accuracy, GSFE curves on 20 distinct planes are calculated in each alloy. Additionally, we calculated the GSFE curves (not shown here) by shifting two halves of the cell with respect to each other continuously by 20 lattice periodicities within the same plane, but the results are different from those based on distinct planes, especially for the CSRO structures. Within the GSFE assessments, the calculations of USFE and intrinsic stacking fault energy (ISFE) are vital. USFE represents the peak energy barrier against dislocation nucleation, directly correlating to the alloy's yield strength, while ISFE provides insight into the energy landscape post-slip.

For CoCrNi the GSFEs were computed along the crystallographic $\langle 112 \rangle$ direction where the orientations of *x*, *y*, and *z* were [110], [112], and [111], respectively, taking into account both random and CSRO structures, whereas the GSFEs of MoNbTa and the two quinaries (HfMoNbTaTi and HfNbTaTiZr) were calculated along the $\langle 111 \rangle$ direction on {110} planes, using simulation cells with orientations of *x*[112], *y*[111], and *z*[110]. In Figure 7, the mean GSFE curves of random- and CSRO-structured CoCrNi are presented with their standard deviations, with the unstable SFE (γ_{usf}) and intrinsic SFE (γ_{isf}) labeled in the graph. In general, a positive γ_{isf} suggests a stable FCC structure, while a negative γ_{isf}

indicates that the material is more stable in an HCP structure. Our results show that the random structure exhibits a negative γ_{isf} , while the γ_{isf} of the CSRO structure displays a positive value indicating a more stable FCC structure. Experimentally, the presence of a short-range order in FCC CoCrNi has been confirmed [73], aligning with our findings. In Table 2, we observe the USFE and ISFE values for the CoCrNi alloy in both random and CSRO structures using EAM and DFT calculation. The CSRO structures of CoCrNi show a higher USFE and ISFE due to the possibility that the presence of CSRO will raise the energy barriers for dislocation nucleation and motion. On the other hand, the CSRO structure of MoNbTa shows a lower USFE than the random structure (see Table 3). In Table 3, a DFT calculation for the USFE of a random structure is also depicted. Moreover, the USFE value of the SROM random MoNbTa, which is 938.01 mJ/m², is in good agreement with the values found in the ternary MoNbTa that is both random and CSRO structured. This observation aligns with the findings reported by Romero et al. [74].

Table 2. USFE and ISFE (in mJ/m²) of random and CSRO structures of CoCrNi. For the CSRO structures, EAM-based data were from annealing at 350 K, while DFT-based data were from annealing at 500 K.

MPEA	Methods	Structures	USFE	ISFE
CoCrNi	EAM	Random CSRO	310.2019623 346.170945	-14.618608 82.7860395
	DFT	Random CSRO	313 [75]	-42.9 [76] 30 [76]

MPEA	Methods	Structures	USFE
	EAM	Random	865.43
MoNbTa	EAM	CSRO	858.12
	DFT	Random	1054.58106



Table 3. USFE (in mJ/m²) of random and CSRO structures of MoNbTa.

Figure 7. GSFE curves of Random and CSRO structured CoCrNi. The shaded region indicates the stand deviation based on 20 GSFE curves.

In Figure 8a, the HfMoNbTaTi alloy shows a clear decrease in USFE with increasing temperature across all structural states, indicating a reduction in resistance to dislocation motion as thermal agitation increases. A similar trend is observed in Figure 8b for the HfNbTaTiZr (random structure), where the USFE decreases as the temperature rises. This is consistent with the typical thermal softening behavior of metals and alloys [41,69,74,77]. Materials usually expand with rising temperatures, increasing the interatomic distances. As a result of this expansion, atomic bonds become weaker and the energy barrier for dislocation movements (as shown by USFE) is lowered. Additionally, rising temperatures

intensify atomic vibrations, which further destabilise the lattice, facilitating the development of dislocations and reducing the USFE. In Figure 8c, the USFEs of four structures of HfNbTaTiZr have been displayed at 0 K where it is evident that the CSRO structures have higher values than the random ones. A similar trend was also followed by the four structures of HfMoNbTaTi (see Figure 8a). For the four MPEAs considered in this study, the GSFEs can be significantly affected by the CSRO, contributing to the observed differences in GSFE between CSRO and random structures [45,78].



Figure 8. Relationship between USFE and temperature of HfMoNbTaTi, HfNbTaTiZr, and pure metals. Data for Mo [48], Nb [48], Ta [65], HfMoNbTaTi [45], and HfNbTaTiZr [45] at 0 K are taken from previous work.

Additionally, Figure 8d showcases the temperature dependence of USFE for pure metals Mo, Ta, Ni, and Nb. The temperature dependence of USFE is significant such that it influences the propensity for cross-slip and twinning behaviors in metals, which are crucial mechanisms for plastic deformation. An increased temperature can lead to more pronounced cross-slip activities [79]. Among the three BCC metals, Mo, with the highest USFE, shows the most substantial resistance to shear deformation at elevated temperatures, while Nb, with the lowest USFE, indicates increased ductility.

4. Conclusions

In this study, we explored the impact of temperature and CSRO on the lattice parameters, elastic constants, and GSFEs of four MPEAs which includes CoCrNi, MoNbTa, HfMoNbTaTi, and HfNbTaTiZr and four pure metals (Mo, Nb, Ta, and Ni). A detailed examination of CSRO structures, annealed at various temperatures, provided deeper insights into the effects of CSRO.

• The investigation revealed that an increase in temperature leads to an expansion in the lattice parameter across all studied MPEAs and pure metals. For CoCrNi

and MoNbTa, the lattice parameters showed minimal variation between CSRO and random structures.

- Consistent with expectations, a temperature rise resulted in a decrease in the stiffness
 of both MPEAs and pure metals, thus reducing their elastic constants. Notably, CSRO
 structures demonstrated greater stiffness relative to random structured MPEAs. The
 trend in elastic constants for both random and CSRO structures was similar, with
 a decrease observed as the temperature increased. Additionally, CSRO structures
 manifested higher GSFEs than random structures.
- Understanding the role of CSRO and temperature in determining material properties allows for the fine-tuning of alloys to achieve desired mechanical properties, including ductility, strength, and resistance to deformation mechanisms like slip and twinning. It supports the development of more accurate models for predicting material behavior, facilitating the exploration of new alloys and composite materials. This work lays a foundational basis for further investigations into the mechanical characteristics of various alloys, encouraging a more in-depth exploration of dislocation dynamics and the effects of elemental concentrations on plastic deformation behavior.

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Appendix A. Structural Parameters and GSFE of MoNbTa Calculated via DFT

To confirm the accuracy of the alloy potential for MoNbTa, this study also conducted DFT calculations to determine the lattice parameters, elastic constants, and GSFE in MoNbTa, as detailed in Tables 1 and 3. These DFT calculations were performed using VASP [80] in its random configuration. Our approach aligns with the methodologies referenced in Refs. [81,82]. For the exchange-correlation energy functional, we employed the Perdew–Burke–Ernzerhof version of the generalized gradient approximation [83]. The Brillouin zone integrations were executed using the Monkhorst–Pack grid [84], applying a smearing width of 0.2 eV as per the Methfessel–Paxton technique [85]. *k*-point meshes of $5 \times 3 \times 8$ and $5 \times 1 \times 8$ were utilized for basic structural parameters and GSFE calculations, respectively.

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