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Deformation of periodic nanovoid structures in Mg single crystals

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Abstract

Large scale molecular dynamics (MD) simulations in Mg single crystal containing periodic cylindrical voids subject to uniaxial tension along the z direction are carried out. Models with different initial void sizes and crystallographic orientations are explored using two interatomic potentials. It is found that (i) a larger initial void always leads to a lower yield stress, in agreement with an analytic prediction; (ii) in the model with $x[\bar{1}100]-y[0001]-z[11\bar{2}0]$ orientations, the two potentials predict different types of tension twins and phase transformation; (iii) in the model with $x[0001]-y[11\bar{2}0]-z[\bar{1}100]$ orientations, the two potentials identically predict the nucleation of edge dislocations on the prismatic plane, which then glide away from the void, resulting in extrusions at the void surface; in the case of the smallest initial void, these surface extrusions pinch the void into two voids. Besides bringing new physical understanding of the nanovoid structures, our work highlights the variability and uncertainty in MD simulations arising from the interatomic potential, an issue relatively lightly addressed in the literature to date.

1. Introduction

Nano/micro-scale voids play an important role in ductile fracture of metallic materials [1]. Subject to tensile loading, voids nucleate from ‘hot spots’ in an otherwise void-free metal, e.g. grain boundaries, precipitate/matrix interfaces; then voids grow and coalesce with each other, forming macroscopically observable cracks and eventually resulting in failure of the material [2]. Even with negligible growth and coalescence, the existence of voids alone may contribute to strain hardening because they are barriers to dislocation movement [3]. Therefore, it is necessary to explore deformation of metals containing voids to elucidate their mechanical responses.

Early work of void growth was conducted in the classical continuum mechanics framework, some of which focused on formulating damage functions [4, 5]. However, it is known that the continuum assumption no longer holds for problems at the nano/micron length scale, e.g., nanovoids, which may exhibit a strong size effect that is not included in local continuum-based constitutive relations. As high-performance computing resources are increasingly accessible to researchers, direct atomistic modeling methods such as molecular dynamics (MD) have become a popular choice in exploring nanovoids in metallic materials, leading to several nanovoid growth mechanisms [6, 7] that are otherwise difficult to identify in *in situ* experiments [8].

Prior atomistic studies revealed that the nanovoid growth process is affected by many factors, including, but not limited to, strain rate [9], temperature [10], initial porosity [11], initial void shape [12], and crystallographic orientations [13–15]. Compared with face-centered cubic (FCC) [1, 10, 12] and body-centered cubic (BCC) [2, 9, 11] systems, there exist much fewer studies of nanovoids in metals with a hexagonal close-packed (HCP) lattice, in part due to a lack of reliable interatomic potential and more complicated slip/twinning systems in the latter. Particularly for HCP Mg, the lightest and the third most abundant element in the Earth’s crust among all metals, most atomistic simulations in the literature concerned nanocracks [16–19]; to the best of our knowledge, only a few MD and atomistic-based multiscale studies have been devoted to nanovoids [20–22]. Since cracks and

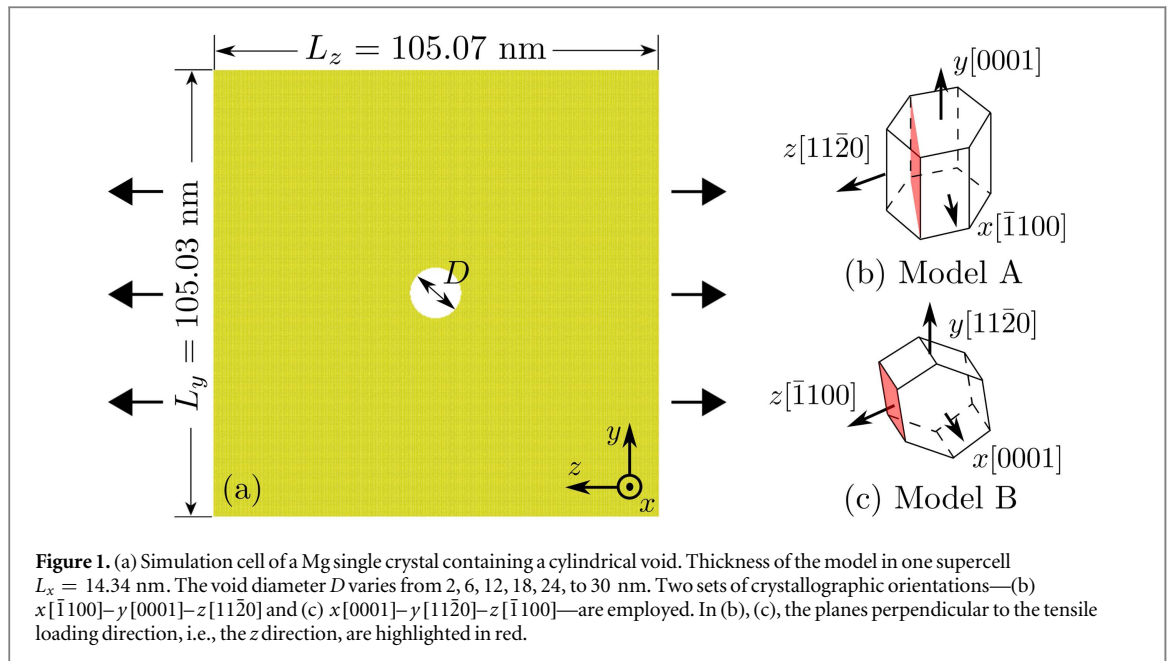


Figure 1. (a) Simulation cell of a Mg single crystal containing a cylindrical void. Thickness of the model in one supercell $L_x = 14.34$ nm. The void diameter D varies from 2, 6, 12, 18, 24, to 30 nm. Two sets of crystallographic orientations—(b) $x[\bar{1}100]-y[0001]-z[11\bar{2}0]$ and (c) $x[0001]-y[11\bar{2}0]-z[\bar{1}100]$ —are employed. In (b), (c), the planes perpendicular to the tensile loading direction, i.e., the z direction, are highlighted in red.

voids affect the mechanical behavior of materials differently [12, 23], physical understanding of voided materials cannot be obtained by extrapolating from that of cracked ones.

While the effects of model size [20], initial porosity [21, 22], strain rate [20–22], temperature [20, 22], crystallographic orientations [20], and interatomic potential [22] have been investigated in voided Mg single crystals, the question remains as to how the initial porosity affects the material deformation in cases of different crystallographic orientations; an exploration of this would shed light on the significance of the elastic anisotropy of materials, a factor often overlooked in previous continuum models. Thus, in this paper, we perform large scale MD simulations to analyze deformation of Mg single crystals containing periodic cylindrical nanovoids as a function of the initial porosity and crystallographic orientations. Since the validity of atomistic-based simulation results heavily hinges on the selection of the interatomic potential [24–26], two potentials are employed with their results compared side-by-side.

2. Methodology

The simulation cell of a Mg single crystal with an initially cylindrical void at the center is shown in figure 1(a). Periodic boundary conditions are applied along all three directions, in effect creating a Mg single crystal with periodic nanovoid structures. Each cuboidal model, containing about 7 million atoms, has edge sizes of $L_x = 14.34$ nm, $L_y = 105.03$ nm, and $L_z = 105.07$ nm. Two sets of crystallographic orientations are employed: $x[\bar{1}100]-y[0001]-z[11\bar{2}0]$ and $x[0001]-y[11\bar{2}0]-z[\bar{1}100]$, referred to as models A and B, respectively. In the two models, the tensile loading direction, i.e., the z direction, is perpendicular to two types of prismatic planes, which are highlighted in red in figures 1(b), (c). The two orientations are chosen because they correspond to the lowest (model A) and the highest (model B) resistances to fatigue crack growth in mode I fracture of Mg among all 10 orientations of interest in the HCP structure [16]. The void diameter D varies from 2 nm, 6 nm, 12 nm, 18 nm, 24 nm, to 30 nm, corresponding to the initial porosity $f_0 = 0.03\%$, 0.26% , 1.02% , 2.31% , 4.10% , and 6.4% , respectively.

Atomistic simulations are conducted using LAMMPS [27]. First, dynamic relaxation at 10 K with an NPT ensemble is performed for 20 ps for the specimen to reach an equilibrium state subject to zero external loading. Then the configuration is energy minimized by iteratively adjusting atoms' positions using the conjugate gradient algorithm. It follows that a homogeneous uniaxial tension is applied on the model along the z axis with an engineering strain rate $\dot{\epsilon}_{zz} = 10^9$ s⁻¹ until the engineering strain $\epsilon_{zz} = 0.15$ is reached; the engineering stress σ_{zz} is calculated using the virial theorem. A constant temperature of 10 K and zero transverse stresses along the x and y directions are maintained with an NPT ensemble. We remark that since the mechanical responses for the two selected crystallographic orientations weakly depend on the temperature [16] and the nanovoid growth mechanism does not change with the strain rate between 10^7 and 10^{10} s⁻¹ [20–22], our simulation results are representative of those at a wide range of temperatures and strain rates. In all dynamic simulations, the time step is 2 fs. Two interatomic potentials—the embedded atom method (EAM) potential by Sun *et al* [28] and the modified embedded atom method (MEAM) potential by Wu *et al* [29], which are considered the most accurate

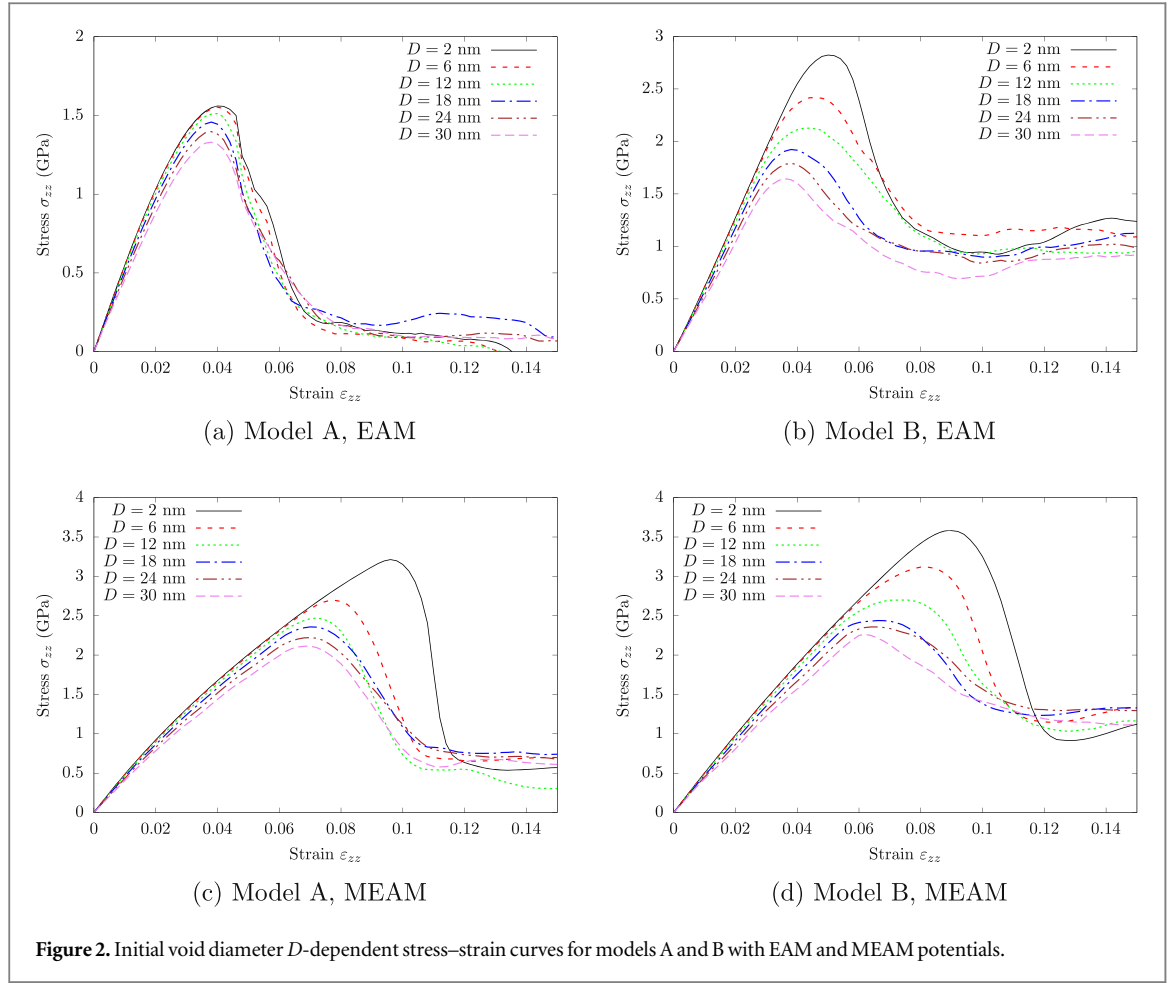


Figure 2. Initial void diameter D -dependent stress–strain curves for models A and B with EAM and MEAM potentials.

in terms of the dislocation core description among all EAM and MEAM potentials for Mg, respectively [29, 30] —are adopted for interactions between Mg atoms. The lattice constant a and the c/a ratio are 3.184 and 1.628 using the EAM potential, while 3.187 and 1.623 using the MEAM potential. Simulation results are visualized using OVITO [31], with the defects identified by the polyhedral template matching (PTM) method [32].

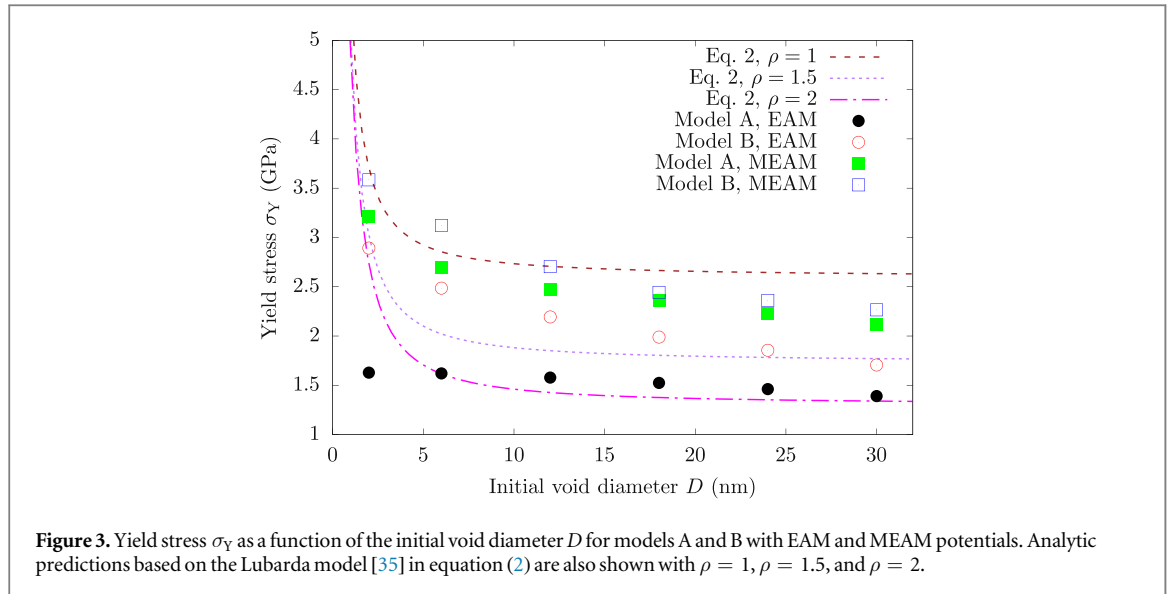
3. Stress–strain response

Stress–strain curves for models A and B with EAM and MEAM potentials, with varying initial void diameter D , are plotted in figure 2. When $D = 2$ nm, Young’s modulus E at $\epsilon_{zz} = 0.01$ of model A is 53.17 GPa (EAM) and 46.6 GPa (MEAM), while that of model B is 63.92 GPa (EAM) and 49.38 GPa (MEAM). Because a Mg single crystal has a low elastic anisotropy index [33], it is safe to assume that it is elastic transverse isotropic. In the meantime, since the two planes normal to the loading direction in two models are different types of prismatic planes, the average Young’s modulus along the transverse direction (i.e., within the basal plane) is 58.545 GPa and 47.99 GPa for EAM and MEAM potentials, respectively. On the other hand, it is known that the Young’s modulus along the same direction in an elastic transverse isotropic media is [34]

$$E = \frac{c_{11}^2 c_{33} + 2c_{13}^2 c_{12} - 2c_{11} c_{13}^2 - c_{33} c_{12}^2}{c_{11} c_{33} - c_{13}^2}, \quad (1)$$

where c_{ij} ($i, j = 1, 2, 3$) are elastic constants, with $c_{11} = 69.6$ GPa (EAM) and 64.3 GPa (MEAM), $c_{12} = 25.3$ GPa (EAM) and 25.5 GPa (MEAM), $c_{13} = 16$ GPa (EAM) and 20.3 GPa (MEAM), and $c_{33} = 69.5$ GPa (EAM) and 70.9 GPa (MEAM). As a result, $E = 58.83$ GPa and 51.86 GPa for EAM and MEAM potentials, respectively, which are close to our MD simulation results.

The yield stresses σ_Y , taken at the initiation of lattice defects, are summarized in figure 3. Also shown are results from an analytic model proposed by Lubarda *et al* [35], i.e.,



$$\sigma_c = \frac{\sqrt{2}bG}{\pi D(1-\nu)} \frac{(1 + 2\sqrt{2}\rho b/D)^4 + 1}{(1 + 2\sqrt{2}\rho b/D)^4 - 1}, \quad (2)$$

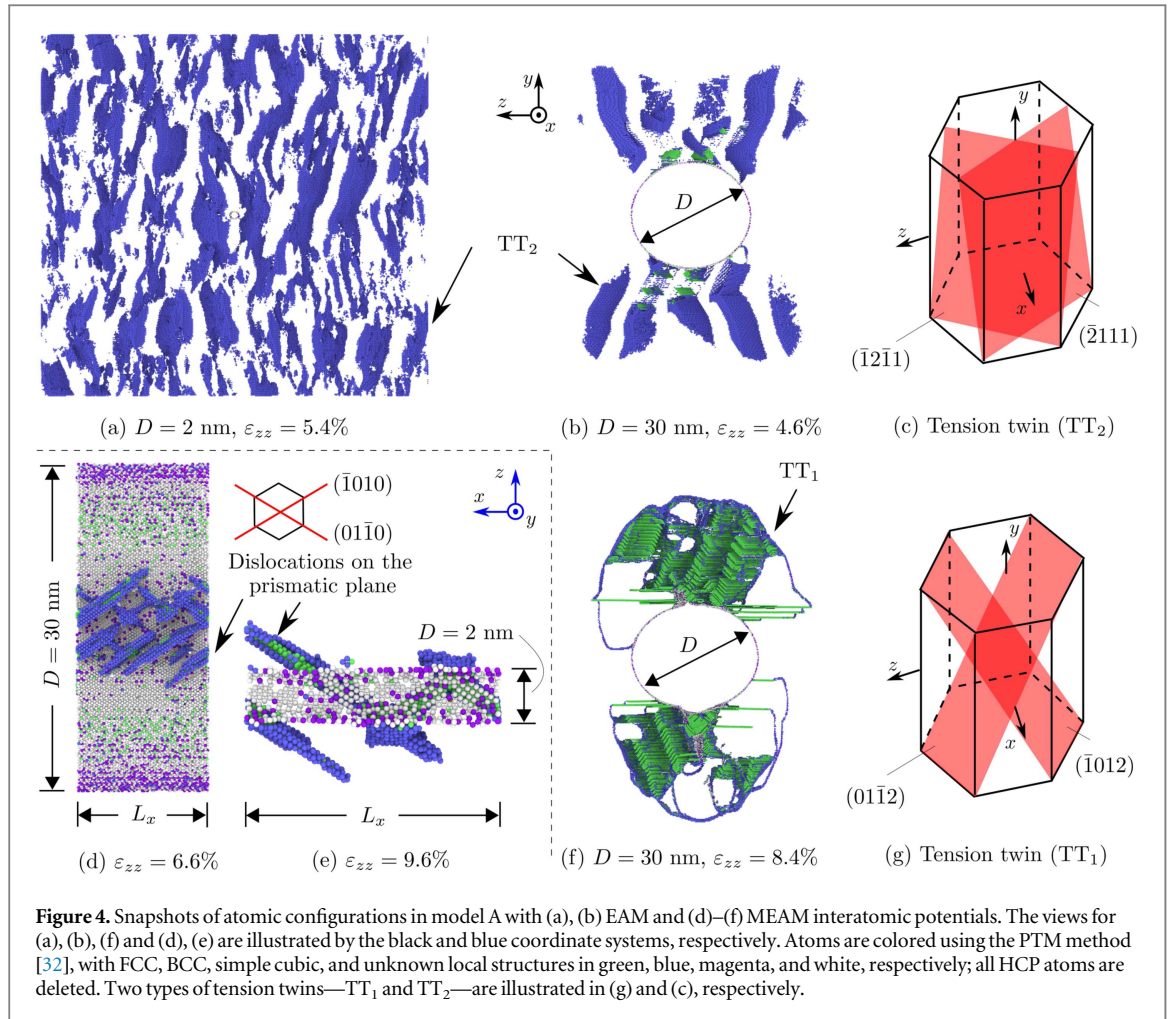
where b is the magnitude of the Burgers vector of the dislocation, G is the isotropic shear modulus, ν is the Poisson's ratio, and ρ is an adjustable parameter with which ρb is the dislocation width. In our case, the two interatomic potentials give, on average, $b = 0.31855$ nm, $G = 25.4$ GPa, and $\nu = 0.22$, whereas b is for the $\langle a \rangle$ dislocation on the prismatic plane which, as will be discussed in the next section, is the only type of dislocations nucleated from the void surface. We remark that the Lubarda model is based on the assumption that only edge dislocations are nucleated from the void surface within an elastic isotropic 2D media subject to uniform biaxial tension under the plane strain condition.

In all cases, a larger D leads to a lower σ_Y , in agreement with the predictions of the Lubarda model [35] between $\rho = 1$ and $\rho = 2$. Both interatomic potentials predict that, with the same D , model B has a higher yield stress than model A, in line with a previous finding that the former has a higher fatigue crack resistance than the latter [16]. For the same model with the same D , the MEAM potential always results in a higher yield stress than the EAM potential. In other words, the MEAM-based predictions are closer to the Lubarda model with $\rho = 1$, while the EAM-based ones are closer to that with $\rho = 2$. On the other hand, previous studies [30, 36] found that the two interatomic potentials predict very similar core structures of dislocations on the prismatic plane, i.e., $\rho \approx 1.5$. Thus, the difference in their yield stress must be attributed to factors other than the dislocation width, suggesting that the Lubarda model with only one adjustable parameter is oversimplified.

4. Defect formation and void evolution

In model A, at the yield point, two types of tension twins— TT_1 and TT_2 , characterized by the twin plane as illustrated in figures 4(c) and (g)—are observed. With the EAM potential, TT_2 on $(\bar{1}2\bar{1}1)$ and $(\bar{2}111)$ planes are nucleated from the void surface, except that when $D = 2$ nm, the tension twins are nucleated homogeneously inside the specimen, as shown in figure 4(a). We remark this exception corresponds to the noticeable deviation of the yield stress for $D = 2$ nm from the Lubarda model prediction compared with the cases of other D (figure 3). For all D , the formation of TT_2 is accompanied by the HCP \rightarrow BCC phase transformation. With the MEAM potential, however, $\langle a \rangle$ edge dislocations on two prismatic planes $(\bar{1}010)$ and $(01\bar{1}0)$ are nucleated from the top and bottom sites of the void surface, before some HCP atoms are transformed to an FCC structure. It follows that Shockley partial dislocations are nucleated inside the FCC region, resulting in TT_1 on $(01\bar{1}2)$ and $(\bar{1}012)$ planes. The coexistence of HCP \rightarrow FCC phase transformation and TT_1 was also reported in two other HCP metals: Zr [37] and Ti [38].

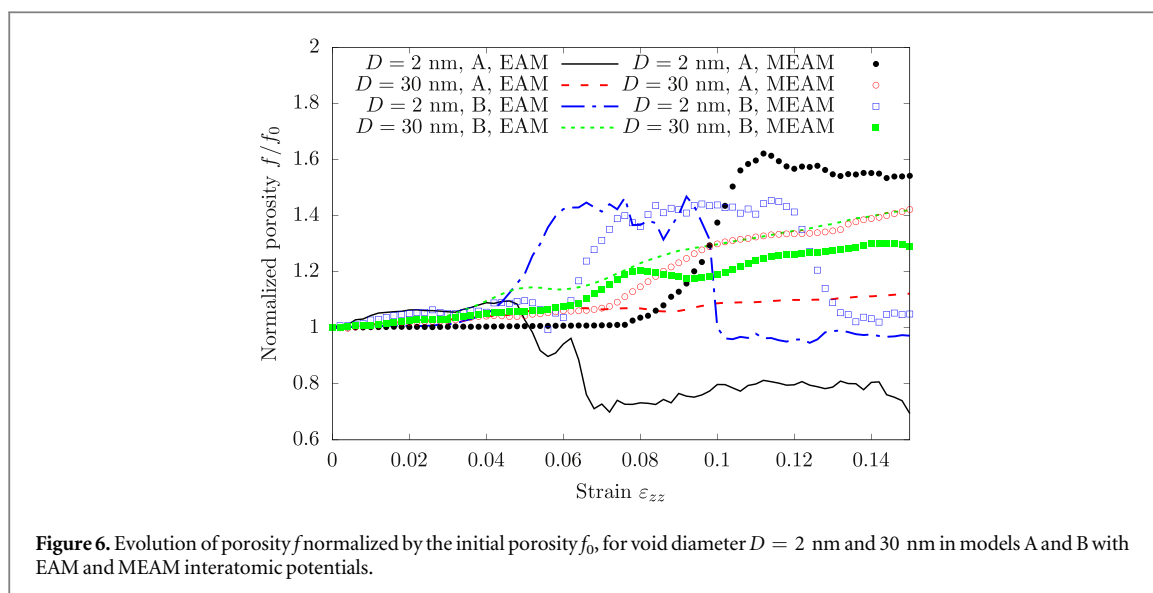
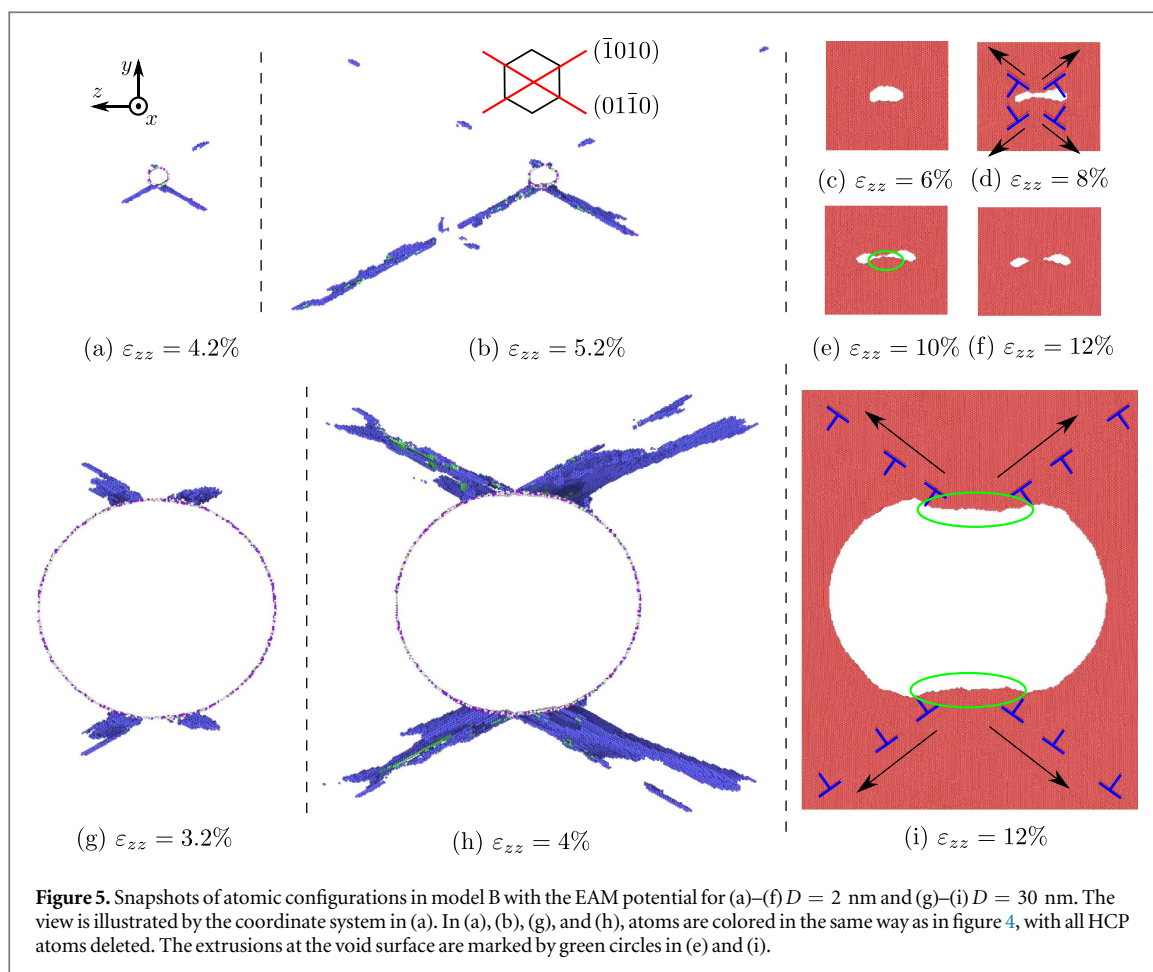
The occurrence of phase transformation and twinning violates the assumption of the Lubarda model that the yielding is solely controlled by the nucleation of edge dislocations from the void surface, yet the analytic predictions inexplicably do not fall too far from the simulation results. Reference [29] studied the TT_1 dislocation using the MEAM potential and found the result in remarkable agreement with the density functional theory calculation. However, we are not aware of any previous investigation of the tension twin using the EAM



potential by Sun *et al* [28]. As a result, we are not able to explain the difference in the tension twin formation between the two interatomic potentials. On the other hand, we note that prior MD simulations [39] using another EAM potential [40] reported that homogeneous nucleation of TT₁ in a Mg single crystal requires a higher critical resolved shear stress (1.5 GPa) than that of TT₂ (0.8 GPa), in alignment with our finding that the MEAM potential predicts a higher yield stress than the EAM potential.

In model B, at the yield point, both EAM and MEAM potentials predict that $\langle a \rangle$ edge dislocations on two prismatic planes ($\bar{1}010$) and $(01\bar{1}0)$ are nucleated from the top and bottom sites of the void surface, as shown in figure 5. No twins are observed at higher strains. Between the two potentials, at 0 K, the Peierls stresses of the edge dislocation on the prismatic plane are 13 and 9.3 MPa using the EAM [30] and MEAM potentials [29], respectively, in contrast to our simulation results that the former leads to a lower yield stress than the latter. This indicates that other quantities, such as the critical stress required to nucleate the dislocation from the void surface, need to be taken into account to justify the potential-dependent difference.

To better examine the void growth, we calculate the porosity, which is found to increase sharply once the defects, either dislocations or twinning, are nucleated, except in model A with $D = 2$ nm using the EAM potential. As described earlier, in this exceptional case (figure 4(a)), tension twins are nucleated homogeneously within the specimen, instead of from the void surface. Subject to further straining, these twins push the materials around the void inward, and reduce the void size/porosity, as illustrated by the black solid line in figure 6. For other D in model A, the void continues growing and maintains a near-elliptic shape up to the maximum strain of 0.15. In model B, as more dislocations glide outward, extrusions are formed and grow at the top and bottom sites of the void. For $D = 2$ nm, the extrusions are large enough to close the central part of the void, resulting in two voids, as shown in figure 5(f), as well as a decrease in the void size, as illustrated by the blue dash-dot line and blue open squares in figure 6. For larger D , there is still one void, yet the extrusions significantly reduce the length of the minor axes (along the y direction) of the elliptic void and the void size growth rate.



5. Conclusion

In this paper, we perform large scale MD simulations to explore initial porosity-, crystallographic orientation-, and interatomic potential-dependent deformation of periodic nanovoid structures in Mg single crystals subject to uniaxial tension along the z direction. Investigations are conducted in the context of stress–strain response, defect formation, and void evolution. The calculated yield stresses are compared with a local continuum-based analytic prediction, whose applicability is also discussed. Main results are summarized as follows:

- (i) For the two models with different crystallographic orientations, both EAM and MEAM potentials predict a lower yield stress for a larger initial void, in reasonably good agreement with the analytic model. For the same initial porosity and orientations, the MEAM potential results in a higher yield stress than the EAM potential.
- (ii) In model A, with $x[\bar{1}100]-y[0001]-z[11\bar{2}0]$ orientations, the first and second types of tension twins, accompanied by HCP \rightarrow FCC and HCP \rightarrow BCC phase transformation, are nucleated from the void surface using the MEAM and EAM potentials, respectively. The exception is that when $D = 2$ nm, the EAM potential predicts homogeneous nucleation of tension twins within the specimen, instead of from the void surface; as a result, the void size decreases after yielding in this particular case. For other D , the void size increases sharply on the threshold of plasticity and continues growing up to the maximum strain while the void maintains a near elliptic shape.
- (iii) In model B, with $x[0001]-y[11\bar{2}0]-z[\bar{1}100]$ orientations, both EAM and MEAM potentials predict that $\langle a \rangle$ edge dislocations on the prismatic planes are nucleated from the void surface. As more dislocations glide away from the void, extrusions are formed at its top and bottom sites. When $D = 2$ nm, the extrusions are large enough to pinch the void into two voids. For other D , the void size remains approximately invariant after certain strain, with its minor axis along the transverse y direction much shorter than that in model A.

Besides bringing new physical understanding of materials with periodic nanovoid structures, our work emphasizes the significance of the interatomic potential in atomistic modeling, which is a powerful tool but also a dangerous one, as it is very easy to set up a simulation ‘incorrectly’. In practice, researchers usually seek to employ the best potential to minimize the ‘incorrectness’. However, it is not always clear which potential is the best because they were, more often than not, fit to limited experimental and *ab initio* data while the quantities relevant for desired simulations may not be considered. Thus, the ‘incorrectness’ may be regarded as variability arising from uncertainty in model parameters. Indeed, the issue of uncertainty quantification and propagation is vitally important even for skilled atomistic modelers, and one of the key points of this paper is to shed light on implications for variability of predictions related to nanovoid structures.

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